Chapter 14

Deadlock Control in Generalized Petri Nets

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ABSTRACT

This chapter proposes a number of deadlock prevention policies for a class of generalized Petri nets, namely G-systems, which is usually considered to be the most generalized Petri nets that can model Flexible Manufacturing Systems (FMSs) with machining, assembly, and disassembly operations. First, a deadlock prevention policy based on elementary siphons theory is presented, which indicates that structural complexity and behavioral permissiveness can be improved effectively. In order to reduce the computational complexity, a Mixed Integer Programming (MIP)-based deadlock detection approach is proposed, then two deadlock control policies combined with MIP method are introduced. Finally, comparison among deadlock prevention policies reported in this chapter is done in terms of structural complexity, behavioral permissiveness, and computational complexity of the resulting supervisor through a typical case study. Importantly, future research directions related to this area are presented at the end of this chapter.

1. INTRODUCTION

Deadlock problems can cause unnecessary costs because of long downtime and low use of some critical and expensive resources in a Flexible Manufacturing System (FMS). Over the last two decades, a great deal of research has been focused on solving deadlock problems in an FMS, receiving an enormous amount of attention (Ezpeleta et al. 1995; Huang, 2007; Iordache and Antsaklis, 2006; Li and Zhou, 2004; Li et al. 2008; Park and Reveliotis, 2001; Uzam and Zhou, 2006; Wu and Zhou, 2007). Specially, deadlock prevention is considered to be one of most effective methods in deadlock control, which is usually achieved by adding monitors to ensure that deadlocks can never occur. In this case, the computation is carried out off-line in a static way and once the control policy...
is established, the system can no longer reach deadlock states. Due to its advantage, deadlock prevention in generalized Petri nets has resulting in various fruits in deadlock control (Chao, 2009; Li and Hu, 2007; Li and Zhao, 2008; Zhao and Li, 2009; Zhao et al. 2010). Since most deadlock prevention policies are developed according to the relationship between liveness and siphons, the siphon-based control methods (Barkaoui and Pradat-Peyre, 1996; Chao, 2007; Chu and Xie, 1997; Reveliotis, 2007) play an important role in the development of liveness-enforcing Petri net supervisors for an FMS. Meanwhile, since the generalized Petri nets have good ability of modeling with multiple resource requirements, it can be used to model more general automated manufacturing systems. Therefore, the deadlock control in a generalized net is much more complicated than ordinary nets. From the points of structural complexity, computational complexity and behavioral permissiveness, it is necessary to facilitate engineers in choosing a suitable control method for industrial application.

This chapter intends to present and compare a variety of siphon-based deadlock prevention policies for $G$-systems, a class of generalized Petri nets, which can model many flexible manufacturing systems. The deadlock control in a generalized net is much more complicated than ordinary nets. From the points of structural complexity, computational complexity and behavioral permissiveness, it is necessary to facilitate engineers in choosing a suitable control method for industrial application.

This section defines a class of Resource Allocation Systems (RAS), namely $G$-systems (Zouari and Barkaoui, 2003) that can be viewed as a Petri net describing a general problem arising in many contemporary application domains such as FMS and workflow management systems. As far as the authors know, this is the most general manufacturing-oriented Petri net subclass in the literature. From manufacturing point of view, it consists of a set of a finite number of shared resources types and a set of a finite number of part types that the system must produce using resources. A $G$-system can well model an FMS with process flexibility, assembly and disassembly operations, assignment flexibility, and permutation flexibility. The more details in definitions of $G$-systems are given as follows.

**Definition 1 (Zouari and Barkaoui, 2003):** A $G$-task is a net $GT=(N, M_i, M_o)$, where

1. $N=(P, T, F, W)$ is a circuit-free net with two special places $i$ and $o$. Place $i$ is a source place with $i^*\cap\emptyset$; and $o$ is a sink place with $o^*\cap\emptyset$.
2. The augmented net $N^*$ is obtained from $N$ by adding a transition $t^*$ such that $o^*\cap\emptyset\{t^*\}$

The rests of this chapter are organized as follows. Section 2 introduces the basic definitions of $G$-systems. An elementary siphon-based deadlock prevention method is developed in Section 3. Section 4 proposes two deadlock prevention methods by using MIP-based deadlock detection method. A case study is given in Section 5 to demonstrate the proposed method. Conclusions and future research directions are finally presented.

### 2. AN APPLICATION SUBCLASS OF GENERALIZED PETRI NETS

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