INTRODUCTION

Integrity constraints (or simply “constraints”) are formal representations of invariant conditions for the semantic correctness of database records. Constraints can be expressed in declarative languages such as datalog, predicate logic, or SQL. This article highlights the historical background of integrity constraints and the essential features of their simplified incremental evaluation. It concludes with an outlook on future trends.

BACKGROUND

Integrity has always been an important issue for database design and control, as attested by many early publications (e.g., Bernstein & Blaustein, 1982; Bernstein, Blaustein, & Clarke, 1980; Codd, 1970, 1979; Eswaran & Chamberlin, 1975; Fraser, 1969; Hammer & McLeod, 1975; Hammer & Sarin, 1978; Nicolas, 1978, 1982; Wilkes, 1972); later ones are too numerous to mention. Expressing database semantics as invariant properties persisting across updates had first been proposed by Minsky (1974). Florentin (1974) suggested expressing integrity constraints as predicate logic statements. Stonebraker (1975) proposed formulating and checking integrity constraints declaratively as SQL-like queries.

Functional dependencies (Armstrong, 1974; Codd, 1970) are a fundamental kind of constraints to guide database design. Referential integrity has been part of the 1989 SQL ANSI and ISO standards (McJones, 1997). The SQL2 standard (1992) introduced the CHECK and ASSERTION constructs (i.e., table-bound and table-independent SQL query conditions) as the most general means to express integrity constraints declaratively (Date & Darwen, 1997). Since the 1990s, uniqueness constraints, foreign keys, and complex queries involving EXISTS and NOT became common features in commercial databases. Thus, arbitrarily general and complex integrity constraints can now be expressed and evaluated in most relational databases. However, most of them offer efficient
support only for the following three simple kinds of declarative constraints:

- **Domain Constraints**: Restrictions on the permissible range of attribute values of tuples in table columns, including scalar SQL data types and subsets thereof, as well as options for default and null values.

- **Uniqueness Constraints**: As enforced by the UNIQUE construct on single columns, and UNIQUE INDEX and PRIMARY KEY on any combination of one or several columns in a table, preventing multiple occurrences of values or combinations thereof.

- **Foreign Key Constraints**: For establishing a relationship between the tuples of two tables, requiring identical column values. For instance, a foreign key on column `emp` of relation `works_in` requires that the `emp` value of each tuple of `works_in` must occur in the `emp_id` column of table `employee`, and that the referenced column (`emp_id` in the example) has been declared as primary key.

For more general constraints, SQL manuals usually recommend using procedural triggers or stored procedures instead of declarative constructs. This is because such constraints may involve nested quantifications over huge extents of several tables. Thus, their evaluation can easily become prohibitively costly. However, declarativity does not need to be sacrificed for efficiency, as shown by many methods of simplified integrity checking as cited in this survey. They are all based on the seminal paper (Nicolas, 1982).

**Simplified Incremental Integrity Checking**

A common idea of all integrity checking methods is that not all constraints need to be evaluated, but at most those that are possibly affected by the incremental change caused by database updates or transactions. Anticipating updates by patterns, most incremental integrity checking methods allow for simplifications of constraints to be generated already at schema compilation time. Such compiled simplifications are parametric conditions to be instantiated, possibly further optimized, and evaluated upon given update requests. For generating them, only the database schema, the integrity constraints, and the update patterns are needed as input. Their evaluation, however, may involve access to the stored data at update time. Methods that generate compiled simplifications are described, for example, by Christiansen and Martinenghi (2006), Decker (1987), and Leuschel and De Schreye (1998). For unanticipated ad-hoc updates, the generation of simplifications takes place at update time. Optimizations for efficient evaluation of simplified constraints are addressed, for example, by Sheu & Lee (1987).

Simplifications can be distinguished by the database state in which they are evaluated. Post-test methods must evaluate their simplifications in the new, updated state, for example, Decker and Celma (1994), Grant and Minker (1990), Lloyd, Sonenberg, and Topor (1987), Nicolas (1982), and Sadri and Kowalski (1988). Pre-test approaches, for example, Bry, Decker, and Manthey (1988), Christiansen and Martinenghi (2006), Hsu and Imielinski (1985), McCune and Henschen (1989), and Qian (1988), only access the old state before the update, that is, they need not execute the update prematurely, since undoing an updated state if integrity is violated is costly. In case of integrity violation, the eagerness of pre-tests to avoid rollbacks is a clear performance advantage over post-tests.

For convenience, a finite set of constraints imposed on a database $D$ is called an *integrity theory* of $D$. For a database $D$ and an integrity theory $IC$, let $D(\text{IC}) = \text{satisfied}$ denote that $IC$ is satisfied in $D$, and $D(\text{IC}) = \text{violated}$ that it is violated. Further, for an update $U$, let $D^U$ denote the updated database. Any simplification method